



SPSS



Statistics for  
Data Analysis



FREE  
WEBINAR

# Chi Square with Statistics for Data Analysis

OCTOBER 1<sup>st</sup> 

10.30 am 

# WEBINAR AGENDA

About Us

Statistics for Data  
Analysis

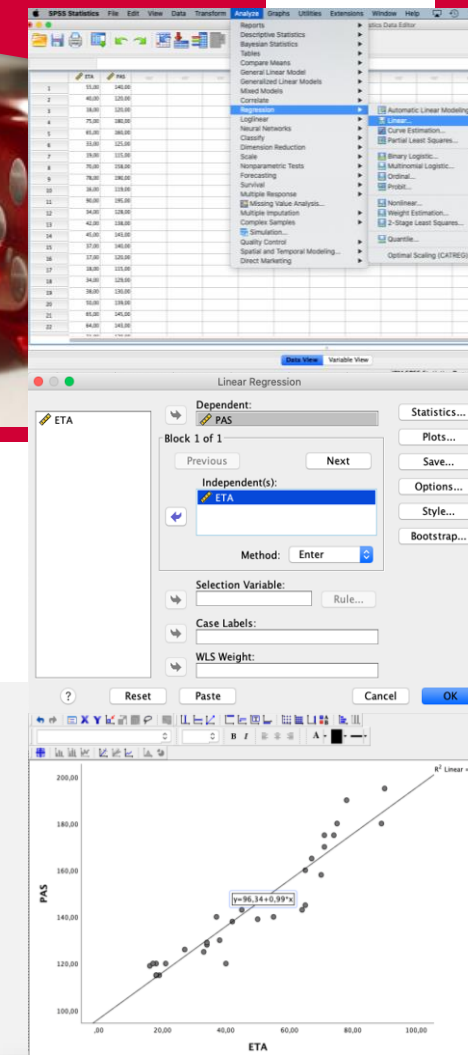
Chi-Square with Statistics  
for Data Analysis

30 years of history... in brief



Services included in the  
solution (LaunchBox, Add-  
On, APP, webinar, Support,  
...)

- Introduction
- Chi-Square Test: theory
- Examples with Statistics  
for Data Analysis
- Q&A
- Acknowledgment

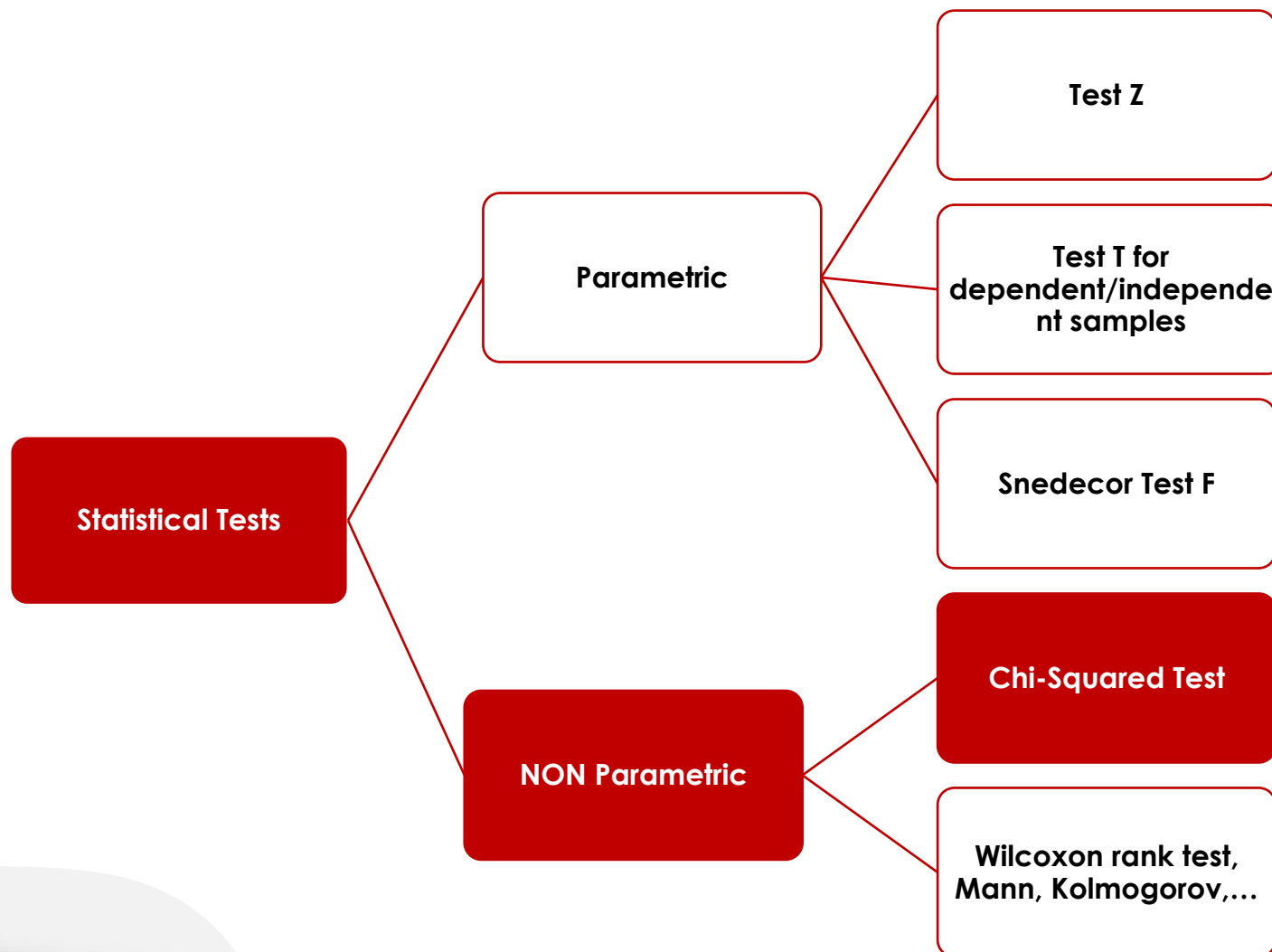


Scarica la nostra APP sugli store



# Chi-Square with Statistics for Data Analysis

## Introduction



# 1) Contingency tables: what about?

Contingency tables are a particular type of cross-tabulations used in statistics to represent and analyze the relationships between two or more variables. They show the joint frequencies of the variables.

| $X \backslash Y$ | $y_1$         | $y_2$         | $\dots$ | $y_j$         | $\dots$ | $y_k$         | Totale        |
|------------------|---------------|---------------|---------|---------------|---------|---------------|---------------|
| $x_1$            | $n_{1,1}$     | $n_{1,2}$     | $\dots$ | $n_{1,j}$     | $\dots$ | $n_{1,k}$     | $n_{1,\cdot}$ |
| $x_2$            | $n_{2,1}$     | $n_{2,2}$     | $\dots$ | $n_{2,j}$     | $\dots$ | $n_{2,k}$     | $n_{2,\cdot}$ |
| $\dots$          | $\dots$       | $\dots$       | $\dots$ | $\dots$       | $\dots$ | $\dots$       | $\dots$       |
| $x_i$            | $n_{i,1}$     | $n_{i,2}$     | $\dots$ | $n_{i,j}$     | $\dots$ | $n_{i,k}$     | $n_{i,\cdot}$ |
| $\dots$          | $\dots$       | $\dots$       | $\dots$ | $\dots$       | $\dots$ | $\dots$       | $\dots$       |
| $x_h$            | $n_{h,1}$     | $n_{h,2}$     | $\dots$ | $n_{h,j}$     | $\dots$ | $n_{h,k}$     | $n_{h,\cdot}$ |
| Totale           | $n_{\cdot,1}$ | $n_{\cdot,2}$ | $\dots$ | $n_{\cdot,j}$ | $\dots$ | $n_{\cdot,k}$ | $n$           |

## 2) Hypothesis structure in a statistical test:



# Chi-Square with Statistics for Data Analysis

## Theory

$$H_0: n_{ij} = n_{ij}^* \forall i, j$$

$$H_1: n_{ij} \neq n_{ij}^* \text{ for at least one couple of } i, j$$

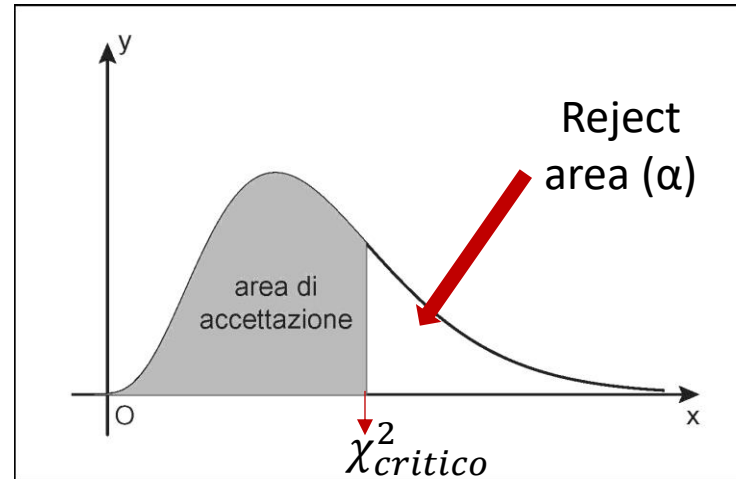


$H_0$ : variables NOT connected (independent)  
 $H_1$ : connection between variables

$$n_{ij}^*(\text{theoretical}) = \frac{n_{i.} \cdot n_{.j}}{n}$$


$$\chi^2 = \sum_i \sum_j \frac{(n_{ij} - n_{ij}^*)^2}{n_{ij}^*} \approx (I - 1) * (J - 1) \text{ gdl}$$

- Accept  $H_0$  if p-value  $> 0.05$
- Reject  $H_0$  if p-value  $\leq 0.05$



|                    | Value                | df | Asymptotic<br>Significance (2-<br>sided) |
|--------------------|----------------------|----|------------------------------------------|
| Pearson Chi-Square | 7989,91 <sup>a</sup> | 2  | <,001                                    |
| Likelihood Ratio   | 9183,186             | 2  | <,001                                    |
| N of Valid Cases   | 25976                |    |                                          |

**Significant Test (reject Ho)**

|            | <u>Smoke</u> | <u>No Smoke</u> | <b>TOT</b> |
|------------|--------------|-----------------|------------|
| <b>M</b>   | 5            | 5               | 10         |
| <b>F</b>   | 10           | 10              | 20         |
| <b>TOT</b> | 15           | 15              | 30         |



**Gender and  
Smoke are  
independent!  
(equal  
proportions)**

|            | <u>Smoke</u> | <u>No Smoke</u> | <b>TOT</b> |
|------------|--------------|-----------------|------------|
| <b>M</b>   | 7            | 3               | 10         |
| <b>F</b>   | 2            | 8               | 10         |
| <b>TOT</b> | 9            | 11              | 20         |



**Gender and  
Smoke are  
dependent! (yes  
connection)**

**McNemar test:** used to determine if there is a difference between proportions of paired samples! (for example, when proportions concerning the same individuals are evaluated with different tests or with the same test but at different times).

|            |          | Test 1post |          |
|------------|----------|------------|----------|
|            |          | Negative   | Positive |
| Test 1 pre | Negative | a          | b        |
|            | Positive | c          | d        |



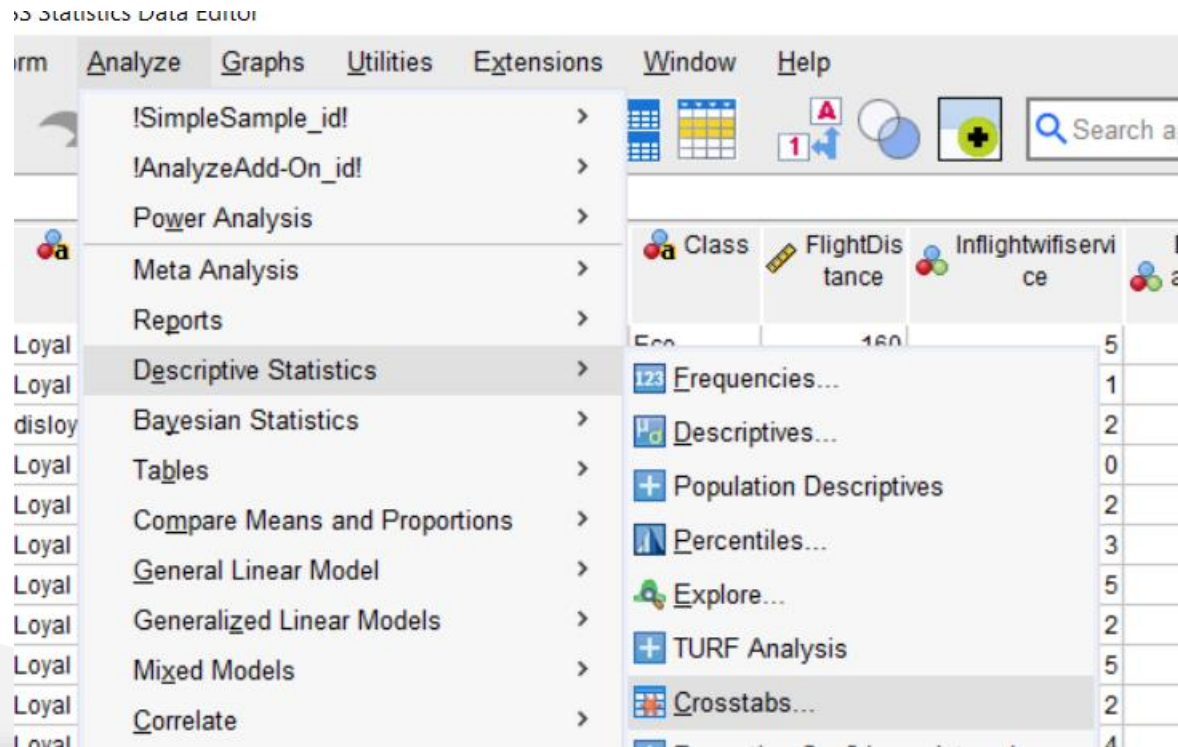
$$\chi_M^2 = \frac{(|b - c| - 1)^2}{b + c} \approx 1 \text{ gdl}$$

If significant → there is a significant difference between the 2 tests, meaning there is a significant deviation on the secondary diagonal! (Note: the McNemar test needs a 2x2 square matrix to be applied).

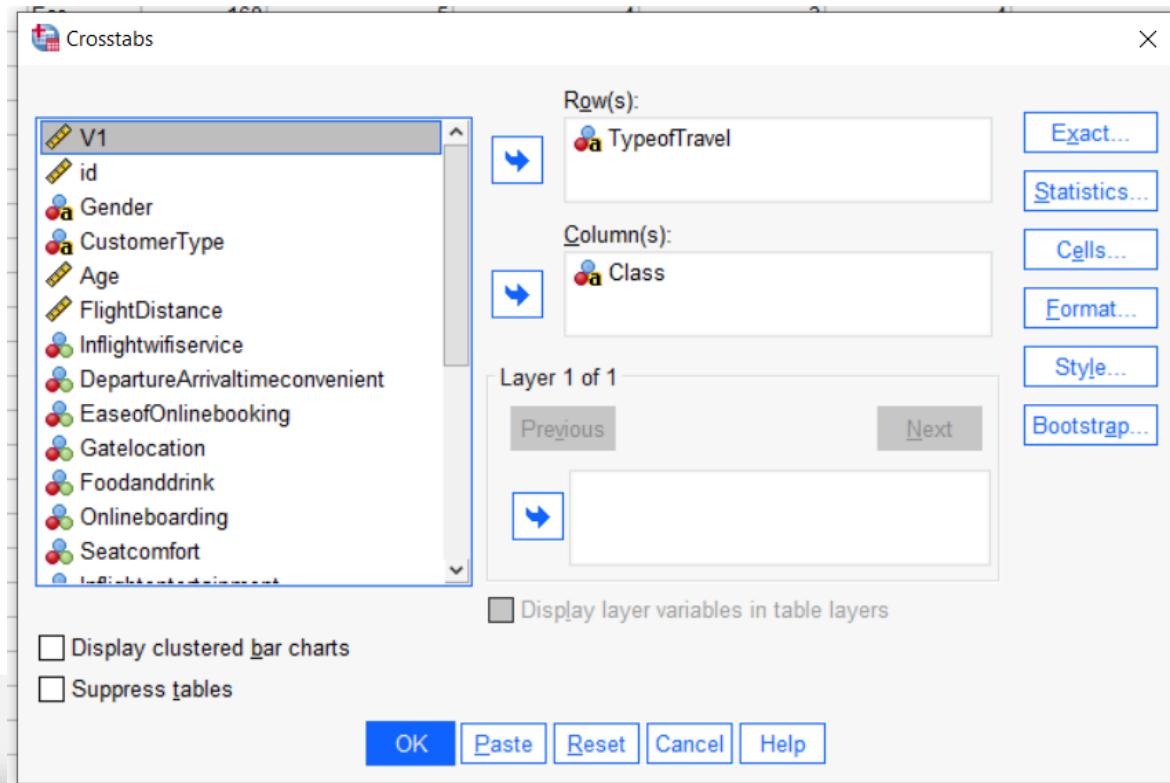
# Chi-Square with Statistics for Data Analysis

## Examples

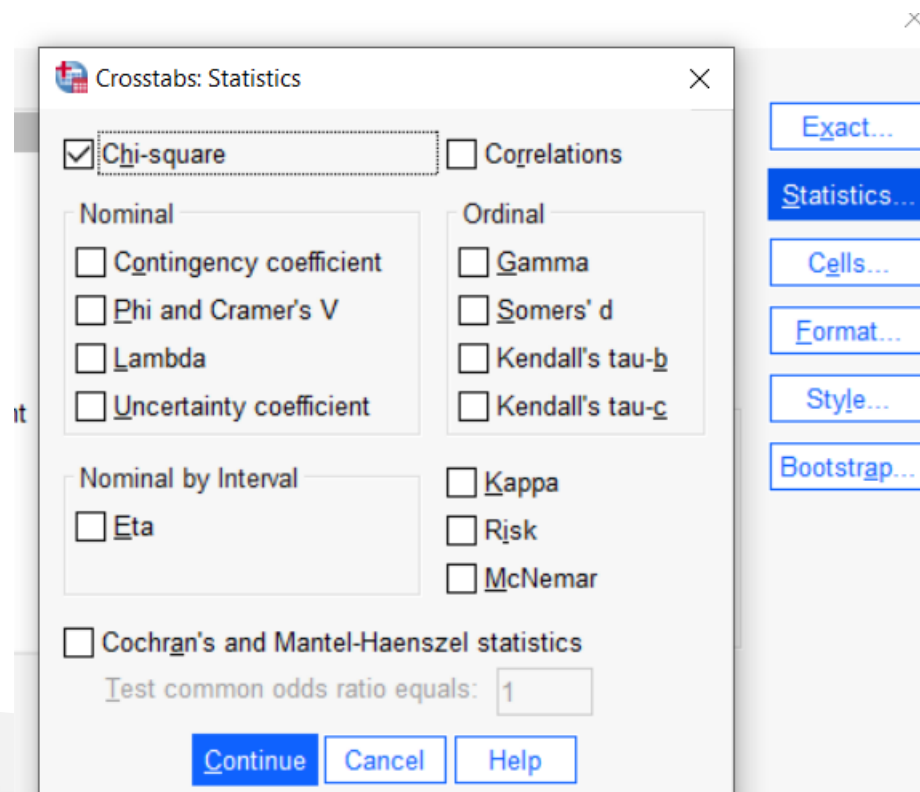
1) Analyze → Descriptive Statistics → Crosstabs



## 2) Crosstabs menu



2.1) Click on «Statistics» button  
and check «Chi-square»



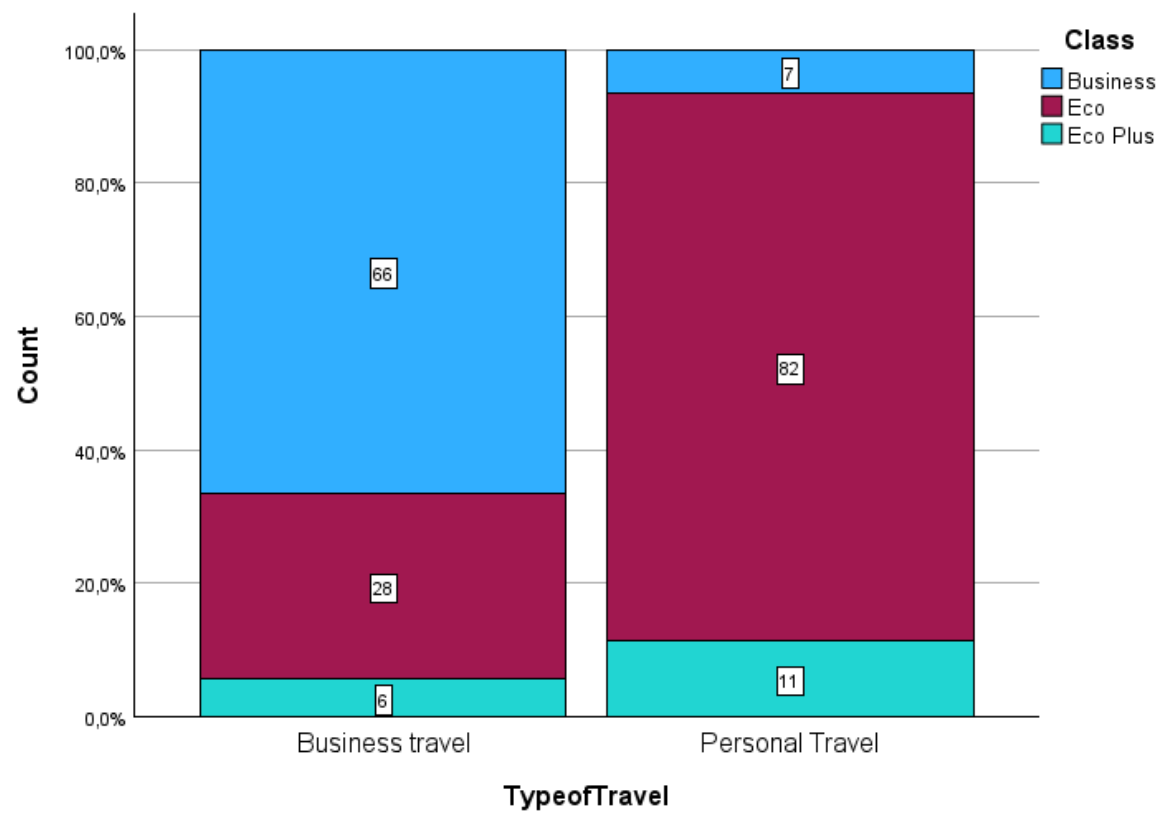
### 3.1) Output

|                    | Value                | df | Asymptotic<br>Significance (2-<br>sided) |
|--------------------|----------------------|----|------------------------------------------|
| Pearson Chi-Square | 7989,91 <sup>a</sup> | 2  | <,001                                    |
| Likelihood Ratio   | 9183,186             | 2  | <,001                                    |
| N of Valid Cases   | 25976                |    |                                          |

**Significant Test (reject Ho)**

### 3.2) Output: barplot

stacked



# Chi-Square with Statistics for Data Analysis

**Conclusion**

- ✓ **Chi-square is a non-parametric test**
- ✓ **It does not require assumptions to be applied**
- ✓ **OK with qualitative variables**
- ✓ **OK for evaluating association/connection between two variables**
- ✓ **For paired data (the same sample in different time-period):  
McNemar test**